

ALNUTH

ALgebraic NUmber THeory and an interface to the KANT System

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Kant part

This package incorporates an interface to some functions of the computer algebra system Kant. Kant is developed by Michael Pohst and his group at the Technische Universität Berlin. The Kant system itself is not part of this interface. It can be obtained at

`www.math.tu-berlin.de/~kant/kash.html`

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1

Introduction

A number field is a finite extension of the field of rational numbers. This package provides various methods to compute with number fields which are given by a defining polynomial or by generators. For background on number fields we refer to [ST79].

Some of the methods provided in this package are written in Gap code. The other part of the methods is imported from the Computer Algebra System KANT [DCK+97]. Hence this package contains some Gap functions and an interface to some functions in the computer algebra system KANT. Therefore one has to have installed KANT to use the full functionality of this package. Furthermore the interface only runs with the Linux version of Gap.

We note that not all available functions of KANT are linked to Gap and the KANT system provides much more methods for computations in number fields.

The main methods included in this package are: creating a number field, computing its maximal order (using KANT), computing its unit group (using KANT) and a presentation of this unit group, computing the elements of a given norm of the number field (using KANT) and determining a presentation for a finitely generated multiplicative subgroup (using KANT). For background on algorithms for number fields we refer to [Poh93], [PZ89] and [Coh93].

The functions provided by this package are introduced in the following chapter. Then an example application is outlined. In the final chapter of this manual the installation of the package is described. We note that the computer algebra system KANT itself is not included in the package.

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Methods for number fields

An algebraic number field is a finite-dimensional extension of the rational numbers \mathbb{Q} . Such a number field has a primitive element and it can be defined by the minimal polynomial of this primitive element. Another important way to define an algebraic number field is by a set of rational matrices which generate a number field.

2.1 Creation of number fields

We provide functions to create number fields defined by rational matrices or by rational polynomials.

- 1 ► `FieldByMatricesNC(matrices)`
 - `FieldByMatrices(matrices)`

Creates a field generated by the rational matrices *matrices*. In the faster NC version, the function assumes that the input generates a field and there are no checks on this performed.

- 2 ► `FieldByMatrixBasisNC(matrices)`
 - `FieldByMatrixBasis(matrices)`

Creates a field with basis *matrices*. The list *matrices* must consist of rational matrices which form a basis for a number field. In the faster NC version, the function assumes that the input is a matrix basis for a field and no checks are performed.

- 3 ► `FieldByPolynomialNC(polynomial)`
 - `FieldByPolynomial(polynomial)`

Creates a field defined by *polynomial*. The polynomial *polynomial* must be an irreducible rational polynomial. In the faster NC version, no checks on the input are performed.

2.2 Methods for number fields

We outline a number of functions for number fields.

- 1 ► `PrimitiveElement(F)`
 - `DefiningPolynomial(F)`

Computes a primitive element and a defining polynomial for the given number field. The defining polynomial is the minimal polynomial of the primitive element. Since *F* contains various primitive elements, `PrimitiveElement` tries to find a primitive element which has a minimal polynomial with small coefficients. Via the global variable `PRIM_TEST` the user can decide how many primitive elements will be compared. The default value is 20.

- 2 ► `IsPrimitiveElement(F, a)`

Checks if the given element generates the field.

- 3 ► `DegreeOverPrimeField(F)`

Returns the degree of *F* over the rationals.

- 4 ▶ `EquationOrderBasis(F)`
- ▶ `MaximalOrderBasis(F)`
- ▶ `IsIntegerOfNumberField(F, k)`

These functions return bases for the equation order or the maximal order of the number field F . Also, they allow to check if a given element is an integer in the given number field.

- 5 ▶ `UnitGroup(F)`
- ▶ `IsomorphismPcpGroup(U)`
- ▶ `IsUnitOfNumberField(F, k)`

These functions determine the unit group of F and an isomorphism to a pcp group. (Recall that the unit group of F is a finitely generated abelian group.) The isomorphism can be used for various computations with the unit group. Also, the last function allows to check whether a given element is a unit in F .

- 6 ▶ `ExponentsOfUnits(F, elms)`

This function determines the exponent vectors of the elements in $elms$ with respect to the generators of the unit group of F . If the unit group of F is not known, then the function computes this unit group also.

- 7 ▶ `IsCyclotomicField(F)`

Check whether F is cyclotomic.

- 8 ▶ `NormCosetsOfNumberField(F, norm)`

Returns a description for the set of all elements of norm $norm$ in F . These elements can be written as a finite union of cosets of the unit group of F . The function returns coset representatives for these cosets.

2.3 Presentations of multiplicative subgroups

Suppose that a finite number of invertible elements of a number field are given. Then these elements generate a finitely generated abelian group. However, it is a non-trivial task to provide a presentation for this abelian group. The most useful representation for such groups is as pcp group.

- 1 ▶ `PcpPresentationOfMultiplicativeSubgroup(F, elms)`
- ▶ `IsomorphismPcpGroup(F, elms)`

Determine a pcp presentation for the multiplicative group of $F \setminus \{0\}$ generated by $elms$ and an isomorphism on this presentation. Note, that the method `IsomorphismPcpGroup` is defined in the Polycyclic package [EN00]. We refer to the manual of this package for further background.

- 2 ▶ `Kernel(map)`
- ▶ `ImagesSet(map, fieldelms)`
- ▶ `ImageElm(map, fieldelm)`
- ▶ `PreImagesRepresentative(map, pcpelm)`

These functions can be used to compute with an isomorphism to a pcp presented image. If $fieldelm$ is not contained in the source of map , then the function `ImageElm` returns fail.

In the determination of the Pcp-presentation of a multiplicative subgroup generated by $elms$ the relations between the elements in $elms$ play an important role. Let $elms = \{e_1, \dots, e_l\}$ be a finite subset of a field F . The relation lattice for $elms$ is

$$rl(elms) := \left\{ (h_1, \dots, h_l) \in \mathbb{Z}^l \mid e_1^{h_1} \cdots e_l^{h_l} = 1 \right\}.$$

- 3 ▶ `RelationLattice(F, elms)`

Determines a generating set for the relation lattice of the field elements $elms$.

2.4 Methods to compute with subgroups of the unit group

1 ► RelationLatticeOfUnits(F , $elms$)

Determines a basis for the relation lattice of the units $elms$ in triangularized form. Note that this method is more efficient than the method `RelationLattice`.

2 ► IntersectionOfUnitSubgroups(F , $gen1$, $gen2$)

The lists $gen1$ and $gen2$ are supposed to generate two subgroups U_1 and U_2 of the unit group of F . This function determines the intersection of U_1 with U_2 . The result is returned as a list of vectors generating the lattice $\{e \in \mathbb{Z}^n \mid g_1^{e_1} \cdots g_n^{e_n} \in U_2\}$ for $gen1 = [g_1, \dots, g_n]$.

This function does not check the input for efficiency reasons and it may return wrong results if the input generators do not fulfil the requirements.

2.5 Factorisation of polynomials over a number field

1 ► FactorsPolynomialKant(F , pol)

embeds the rational polynomial pol into the polynomial ring over the number field F , which has to be constructed by `FieldByPolynomial` or `AlgebraicExtension`, and returns the factorization of the embedded polynomial. By default a denotes the primitive element of the field one can obtain from `PrimitiveElement(F)`, i. e. a root of the defining polynomial of F .

```
gap> x := Indeterminate( Rationals, "x" );;
gap> pol := 2*x^7+2*x^5+8*x^4+8*x^2;
2*x^7+2*x^5+8*x^4+8*x^2
gap> L := FieldByPolynomial( x^3-4 );
<algebraic extension over the Rationals of degree 3>
gap> y := Indeterminate( L, "y" );;
gap> FactorsPolynomialKant( L, pol );
[ !2*y, y, y+(a), y^2+!1, y^2+((-1*a))*y+(a^2) ]
```

2.6 Examples

1 ► ExampleMatField(l)

This function returns some examples of fields generated by matrices. There are 9 such example fields provided and they can be obtained by assigning the input l to an integer between 1 and 9. Some of the properties of the examples are summarized in the following table.

	degree over \mathbb{Q}	number of generators	dim. of generators
<code>ExampleMatField(1)</code>	4	4	4
<code>ExampleMatField(2)</code>	4	4	4
<code>ExampleMatField(3)</code>	4	4	4
<code>ExampleMatField(4)</code>	4	13	4
<code>ExampleMatField(5)</code>	4	13	4
<code>ExampleMatField(6)</code>	4	7	4
<code>ExampleMatField(7)</code>	4	18	4
<code>ExampleMatField(8)</code>	4	13	4
<code>ExampleMatField(9)</code>	4	7	4

3 An example application

In this section we outline two example computations with the functions of the previous chapter. The first example uses number fields defined by matrices and the second example considers number fields defined by a polynomial.

3.1 Number fields defined by matrices

```
gap> m1 := [ [ 1, 0, 0, -7 ],
             [ 7, 1, 0, -7 ],
             [ 0, 7, 1, -7 ],
             [ 0, 0, 7, -6 ] ];;

gap> m2 := [ [ 0, 0, -13, 14 ],
             [ -1, 0, -13, 1 ],
             [ 13, -1, -13, 1 ],
             [ 0, 13, -14, 1 ] ];;

gap> F := FieldByMatricesNC( [m1, m2] );
<field in characteristic 0>

gap> DegreeOverPrimeField(F);
4
gap> PrimitiveElement(F);
[ [ 1, 0, 0, -7 ], [ 7, 1, 0, -7 ], [ 0, 7, 1, -7 ], [ 0, 0, 7, -6 ] ]

gap> Basis(F);
Basis( <field in characteristic 0>,
[ [ [ 1, 0, 0, 0 ], [ 0, 1, 0, 0 ], [ 0, 0, 1, 0 ], [ 0, 0, 0, 1 ] ],
  [ [ 0, 1, 0, 0 ], [ -1, 1, 1, 0 ], [ -1, 0, 1, 1 ], [ -1, 0, 0, 1 ] ],
  [ [ 0, 0, 1, 0 ], [ -1, 0, 1, 1 ], [ -1, -1, 1, 1 ], [ 0, -1, 0, 1 ] ],
  [ [ 0, 0, 0, 1 ], [ -1, 0, 0, 1 ], [ 0, -1, 0, 1 ], [ 0, 0, -1, 1 ] ] ] )

gap> MaximalOrderBasis(F);
Basis( <field in characteristic 0>,
[ [ [ 1, 0, 0, 0 ], [ 0, 1, 0, 0 ], [ 0, 0, 1, 0 ], [ 0, 0, 0, 1 ] ],
  [ [ 1, 0, 0, -1 ], [ 1, 1, 0, -1 ], [ 0, 1, 1, -1 ], [ 0, 0, 1, 0 ] ],
  [ [ 1, 0, -1, 0 ], [ 1, 1, -1, -1 ], [ 1, 1, 0, -1 ], [ 0, 1, 0, 0 ] ],
  [ [ 1, -1, 0, 0 ], [ 1, 0, -1, 0 ], [ 1, 0, 0, -1 ], [ 1, 0, 0, 0 ] ] ] )

gap> U := UnitGroup(F);
<matrix group with 2 generators>

gap> u := GeneratorsOfGroup( U );;
```

```

gap> nat := IsomorphismPcpGroup(U);
[ [ [ 0, 1, -1, 0 ], [ 0, 1, 0, -1 ], [ 0, 1, 0, 0 ], [ -1, 1, 0, 0 ] ],
  [ [ 1, 0, -1, 1 ], [ 0, 1, -1, 0 ], [ 1, 0, 0, 0 ], [ 0, 1, -1, 1 ] ] ] ->
[ g1, g2 ]

gap> H := Image(nat);
Pcp-group with orders [ 10, 0 ]
gap> ImageElm( nat, u[1]*u[2] );
g1*g2
gap> PreImagesRepresentative(nat, GeneratorsOfGroup(H)[1] );
[ [ 0, 1, -1, 0 ], [ 0, 1, 0, -1 ], [ 0, 1, 0, 0 ], [ -1, 1, 0, 0 ] ]

```

3.2 Number fields defined by a polynomial

```

gap> x:=Indeterminate(Rationals);
x_1
gap> g:= x^4-4*x^3-28*x^2+64*x+16;
x_1^4-4*x_1^3-28*x_1^2+64*x_1+16

gap> F := FieldByPolynomialNC(g);
<field in characteristic 0>
gap> PrimitiveElement(F);
(a)
gap> MaximalOrderBasis(F);
Basis( <field in characteristic 0>,
[ !1, (1/2*a), (1/4*a^2), (5/7+1/14*a+1/14*a^2+1/56*a^3) ] )

gap> U := UnitGroup(F);
[ !-1, (-3/7+6/7*a+3/28*a^2-1/28*a^3),
  (13/7+25/14*a+1/28*a^2-3/56*a^3), (36/7-9/7*a-2/7*a^2+3/56*a^3) ]
<group with 4 generators>

gap> natU := IsomorphismPcpGroup(U);
[ !-1, (-3/7+6/7*a+3/28*a^2-1/28*a^3),
  (13/7+25/14*a+1/28*a^2-3/56*a^3), (36/7-9/7*a-2/7*a^2+3/56*a^3)
] -> [ g1, g2, g3, g4 ]

gap> elms := List( [1..10], x-> Random(F) );
[ (4-1/2*a-1*a^2+3/2*a^3), (4/5-2/3*a+4/3*a^3), (1+a+2*a^2-1*a^3),
  (3/4+3*a+3*a^2), (-1-1/5*a^3), (-1/4*a-5/3*a^2), (1-1*a+1/2*a^2),
  (4-3/2*a+1/2*a^2), (-2/5+a-3/2*a^2), (-1*a+a^2+2*a^3) ]

gap> PcpPresentationOfMultiplicativeSubgroup( F, elms );
Pcp-group with orders [ 0, 0, 0, 0, 0, 0, 0, 0, 0, 0 ]

gap> isom := IsomorphismPcpGroup( F, elms );
[ (4-1/2*a-1*a^2+3/2*a^3), (4/5-2/3*a+4/3*a^3),
  (1+a+2*a^2-1*a^3), (3/4+3*a+3*a^2), (-1-1/5*a^3),
  (-1/4*a-5/3*a^2), (1-1*a+1/2*a^2), (4-3/2*a+1/2*a^2),
  (-2/5+a-3/2*a^2), (-1*a+a^2+2*a^3) ]
[ (4-1/2*a-1*a^2+3/2*a^3), (4/5-2/3*a+4/3*a^3), (1+a+2*a^2-1*a^3),

```



```

(3/4+3*a+3*a^2), (-1-1/5*a^3), (-1/4*a-5/3*a^2), (1-1*a+1/2*a^2),
(4-3/2*a+1/2*a^2), (-2/5+a-3/2*a^2), (-1*a+a^2+2*a^3) ] ->
[ g1, g2, g3, g4, g5, g6, g7, g8, g9, g10 ]

gap> y := RandomGroupElement( elms );
(-475709724976707031371325/71806328788189775767952976
-379584641261299592239825/13055696143307231957809632*a
-462249188570593771377595/287225315152759103071811904*a^2+
2639763613873579813685/2901265809623829323957696*a^3)

gap> ImageElm( isom, y );
g1^-1*g3^-2*g6^2*g8^-1*g9^-1
gap> z := last;
g1^-1*g3^-2*g6^2*g8^-1*g9^-1

gap> PreImagesRepresentative( isom, z );
(-475709724976707031371325/71806328788189775767952976
-379584641261299592239825/13055696143307231957809632*a
-462249188570593771377595/287225315152759103071811904*a^2+
2639763613873579813685/2901265809623829323957696*a^3)

gap> FactorsPolynomialKant( g, F );
[ x_1+(-40/7+31/7*a+3/7*a^2-1/7*a^3), x_1+(-2+a), x_1+(-1*a),
  x_1+(26/7-31/7*a-3/7*a^2+1/7*a^3) ]

```

4

Installation

This package provides an interface between GAP 4 and KANT respectively KASH, the shell of the computational algebraic number theory system KANT. By now the interface can only be used on a Linux system. KASH itself is not part of this package. It has to be obtained and installed independently of this package. Alnuth works with KASH version 2.4 or 2.5.

4.1 Getting and installing KASH

KASH is available at

www.math.tu-berlin.de/~kant/download.html

Note that you have to download two files for a complete installation of KASH. For the installation of version 2.5 of KASH on a Linux system you would do the following steps:

1. Download the files `kash_2.5.common.tar.gz` and `kash_2.5.3.linux.tar.gz` into the same directory on your system.
2. Unpack the files using `tar`. This will create a directory `KASH_2.5` containing among other files the KASH executable called `kash`.

The place where KASH is located in your system is independent of the place where the Alnuth-package is installed.

4.2 Installing this package

This package is available at

www.icm.tu-bs.de/ag_algebra/software/assmann/Alnuth

in form of a gzipped tar-archive or as an uncompressed tar-archive.

There are two ways of installing the package. If you have permission to add files to the installation of GAP 4 on your system you may install the Alnuth-package into the `pkg` subdirectory of the GAP installation tree. If you do not have the permission to do that you may install the Alnuth-package in your private area. In the latter case you need to have a directory named `pkg` in your private area (for details see 75.1 in the reference manual).

Now move the `alnuth.tar.gz` of `alnuth.tar` file into the directory `pkg` and unpack it:

```
bash> tar xzf alnuth.tar.gz      # for the gzipped tar-archive
bash> tar xf alnuth.tar          # for the uncompressed tar-archive
```

4.3 Adjust the path of the executable for KASH

This package needs to know where the executable for KASH is. In the default setting Alnuth will check if there is an executable called **kash** in your search path (The search path is the set of directories through which your shell looks for executable programs when no absolute path is given. Type `echo $PATH` in your terminal to see which directories are contained in your search path.).

In Section 4.4 we explain how to write a very short shell script, which executes KASH, and indicate how you can assure that Alnuth finds it in the default setting. We recommend to use this default setting. An advantage of this method is, that in case of an installation of a new version of Alnuth you do not have to adjust the path to the executable of KASH again.

If you do not want to use the default setting, then there are two other possibilities.

If you are able to edit the file `pkg/alnuth/defs.g`, then you can change the line

```
BindGlobal( "KANTEXEC", Filename( DirectoriesSystemPrograms( ), "kash" ) );
```

to something like

```
BindGlobal( "KANTEXEC", "mykash/kash -l mykash/lib" );
```

where **mykash** needs to be replaced with the directory where KASH was installed. For example **mykash** could be replaced by `/usr/local/KASH_2.5`. Please note that in case of a new installation of Alnuth you will have to edit the file `pkg/alnuth/defs.g` again. Alternatively you can also change your personal `.gaprc` file (see 3.4 The `.gaprc` file) for setting the variable `KANTEXEC` to a proper value. To do this add the command line mentioned above to `.gaprc`.

The third possibility is to change the path to the executable within GAP using one of the following two functions. To do this you first have to load the package (see Section 4.5).

1 ► `SetKantExecutable(path)`

adjusts the global variable `KANTEXEC` for the current GAP session. Depending on your installation of KASH the string *path* has to be either the command to start KASH in a terminal (for example **kash**) or the complete path to the executable of KASH (for example `/usr/local/KASH_2.5/kash`). In the latter case the library-path does not have to be specified, but is added automatically. Thereby the message

```
kash: hmm, I cannot find 'lib/init.g', maybe use option '-l <libname>'?
```

will appear on the screen, which can be ignored.

To use

2 ► `SetKantExecutablePermanently(path)`

you need to be allowed to overwrite the file `pkg/alnuth/defs.g`. The function does the same as `SetKantExecutable` and changes the file `pkg/alnuth/defs.g` respectively in addition. Thus the value of the global variable `KANTEXEC` is changed permanently. In case of a new installation of Alnuth, you will have to run this command again.

Both functions run a test whether *path* is a valid string for a filename of an executable for KASH version 2.4 or 2.5.

If you want to set the path to the executable of KASH using the function `SetKantExecutable` every time you start GAP, you could add the command line `SetKantExecutable(path)` to your personal `.gaprc` file (see Section 3.4 in the GAP Reference manual).

4.4 How to write a shell script which executes KASH

In this section we explain how to write a shell script which executes KASH. Such a script is needed if you want to use the default setting of Alnuth for the execution of KASH (see Section 4.3).

Switch to your home directory (`cd ~`) and check (using `ls`) if there is a directory called `bin`. If not then create one with `mkdir bin`. Change to the `bin` directory (`cd bin`) and open an empty file called `kash` with an editor of your choice. Add the lines

```
#!/bin/sh
mykash/kash -l mykash/lib
```

where `mykash` needs to be replaced with the directory where KASH was installed. After this your file could look for example like this:

```
#!/bin/sh
/usr/local/KASH_2.5/kash -l /usr/local/KASH_2.5/lib
```

Save the file and close the editor. Then type `chmod u+x kash` in your terminal to make the script executable.

Now we have to assure that the directory `bin` is in your search path. Type `echo $PATH` to check if this is the case. If not then you can add `bin` to the search path by typing

```
bash> export PATH=$PATH:/home/user/bin
```

where `/home/user` needs to be replaced by your home directory. If you want to extend your search path permanently you can add this line to the `.bashrc` file in your home directory.

If you use a c-shell instead of bash, then you have to extend the search path with the command

```
set PATH = ( $PATH /home/user/bin )
```

and edit the file `.cshrc`.

4.5 Loading and testing the package

To use this package you have to request it explicitly. This is done by calling

```
gap> LoadingPackage("alnuth");
Loading Alnuth 2.2.0 ...
true
gap>
```

Once the package is loaded, it is possible to check the correct installation by running the test suite of the package with the command

```
gap> ReadPackage( "alnuth", "tst/testall.g" );
```

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